

```
In[19]:= f = (2 x^3 - 7 x^2 + 2 x - 3) / (x - 3)^2
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -10, 10}]
```

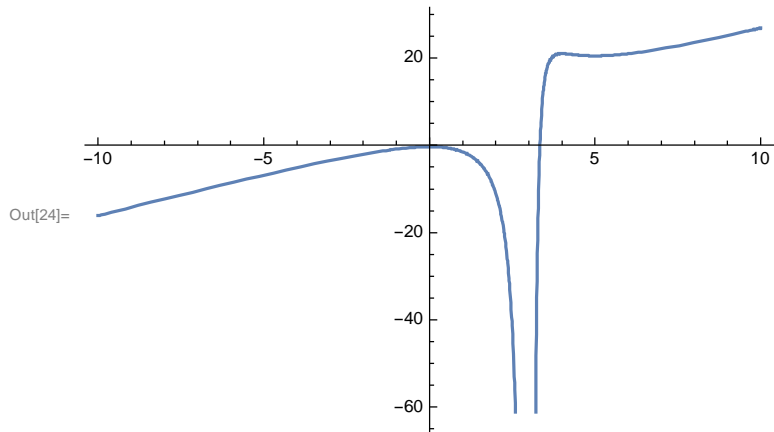
Out[19]= 
$$\frac{-3 + 2x - 7x^2 + 2x^3}{(-3 + x)^2}$$

Out[20]= 
$$\frac{2x(20 - 9x + x^2)}{(-3 + x)^3}$$

Out[21]= {{x → 0}, {x → 4}, {x → 5}}

Out[22]= 
$$\frac{4(-30 + 7x)}{(-3 + x)^4}$$

Out[23]= {{x →  $\frac{30}{7}$ }}



```
In[25]:= f = (2 x^3 + 9 x^2 + 36 x + 36) / (x + 2)^2  
df = D[f, x] // Simplify  
Solve[df == 0, x]  
ddf = D[df, x] // Simplify  
Solve[ddf == 0, x]  
Plot[f, {x, -10, 10}]
```

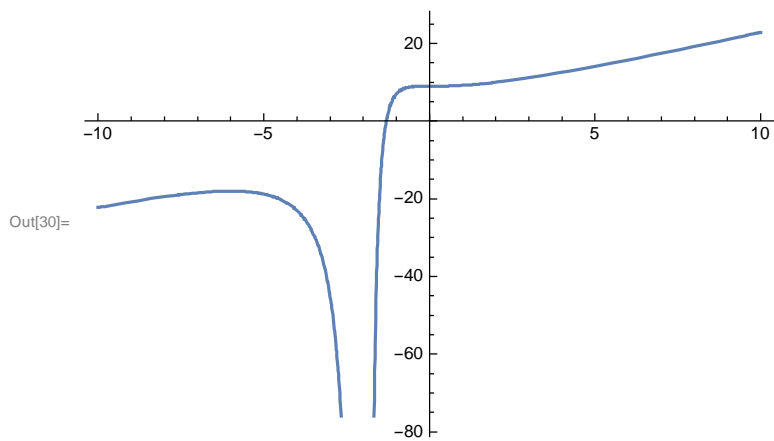
Out[25]= 
$$\frac{36 + 36 x + 9 x^2 + 2 x^3}{(2 + x)^2}$$

Out[26]= 
$$\frac{2 x^2 (6 + x)}{(2 + x)^3}$$

Out[27]=  $\{\{x \rightarrow -6\}, \{x \rightarrow 0\}, \{x \rightarrow 0\}\}$

Out[28]= 
$$\frac{48 x}{(2 + x)^4}$$

Out[29]=  $\{\{x \rightarrow 0\}\}$



```
In[31]:= f = (x^3 + 4 x^2 + 11 x + 11) / (x + 2)^2
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -10, 10}]
```

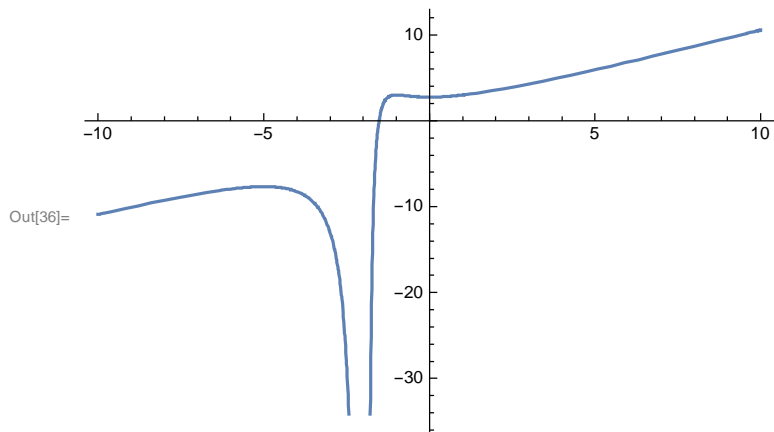
$$\text{Out[31]= } \frac{11 + 11 x + 4 x^2 + x^3}{(2 + x)^2}$$

$$\text{Out[32]= } \frac{x (5 + 6 x + x^2)}{(2 + x)^3}$$

```
Out[33]= {{x -> -5}, {x -> -1}, {x -> 0}}
```

$$\text{Out[34]= } \frac{2 (5 + 7 x)}{(2 + x)^4}$$

```
Out[35]= {{x -> -5/7}}
```



```
In[49]:= f = (8 x^3 - 16 x^2 + 22 x - 11) / (2 (x - 1)^2)
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -5, 5}]
```

$$\text{Out[49]= } \frac{-11 + 22 x - 16 x^2 + 8 x^3}{2 (-1 + x)^2}$$

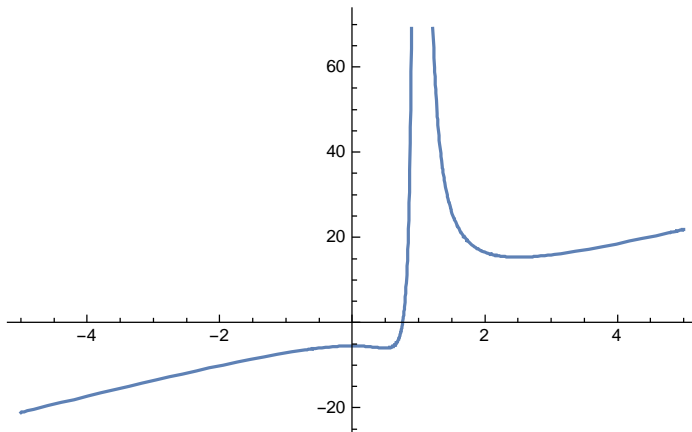
$$\text{Out[50]= } \frac{x (5 - 12 x + 4 x^2)}{(-1 + x)^3}$$

$$\text{Out[51]= } \left\{ \{x \rightarrow 0\}, \left\{x \rightarrow \frac{1}{2}\right\}, \left\{x \rightarrow \frac{5}{2}\right\} \right\}$$

$$\text{Out[52]= } \frac{-5 + 14 x}{(-1 + x)^4}$$

$$\text{Out[53]= } \left\{ \left\{x \rightarrow \frac{5}{14}\right\} \right\}$$

Out[54]=



```

In[67]:= f = (4 x^3 + 25 x^2 + 70 x + 105) / ((x + 3)^2)
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -15, 5}]

```

$$\text{Out[67]= } \frac{105 + 70 x + 25 x^2 + 4 x^3}{(3 + x)^2}$$

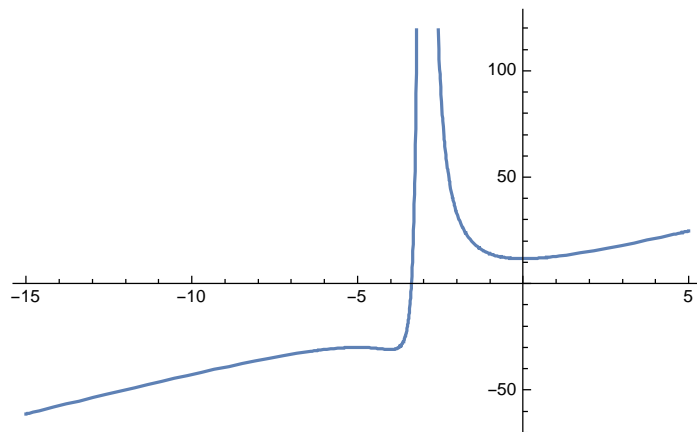
$$\text{Out[68]= } \frac{4 x (20 + 9 x + x^2)}{(3 + x)^3}$$

```
Out[69]= {{x → -5}, {x → -4}, {x → 0}}
```

$$\text{Out[70]= } \frac{8 (30 + 7 x)}{(3 + x)^4}$$

```
Out[71]= {{x → -\frac{30}{7}}}
```

```
Out[72]=
```



```
In[79]:= f = (x^3 + x^2 - 2 x + 1) / ((x - 1) ^ 2)
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -5, 5}]
```

Out[79]= 
$$\frac{1 - 2 x + x^2 + x^3}{(-1 + x)^2}$$

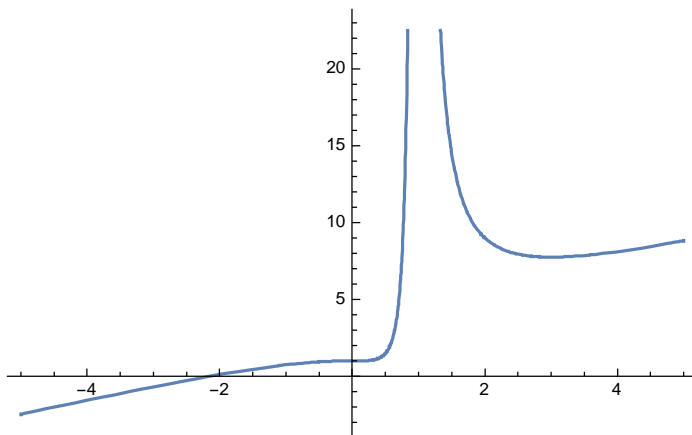
Out[80]= 
$$\frac{(-3 + x) x^2}{(-1 + x)^3}$$

Out[81]= {{x → 0}, {x → 0}, {x → 3}}

Out[82]= 
$$\frac{6 x}{(-1 + x)^4}$$

Out[83]= {{x → 0}}

Out[84]=



```

In[115]:= f = (x^3 + 6 x^2 + 46 x + 69) / ((x + 3) ^ 2)
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -15, 15}]

```

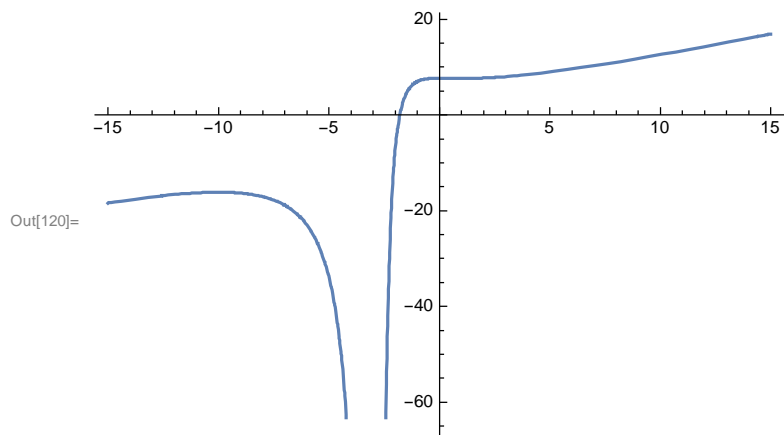
$$\text{Out[115]= } \frac{69 + 46 x + 6 x^2 + x^3}{(3 + x)^2}$$

$$\text{Out[116]= } \frac{x (-10 + 9 x + x^2)}{(3 + x)^3}$$

```
Out[117]= {{x -> -10}, {x -> 0}, {x -> 1}}
```

$$\text{Out[118]= } \frac{-30 + 74 x}{(3 + x)^4}$$

```
Out[119]= {{x -> 15/37}}
```



```

In[109]:= f = (-x^3 + 8 x^2 - 28 x + 42) / ((x - 3)^2)
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -5, 15}]

```

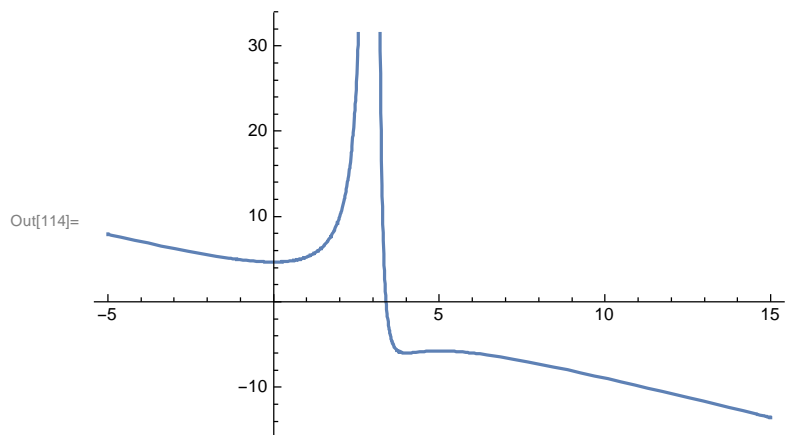
$$\text{Out[109]= } \frac{42 - 28x + 8x^2 - x^3}{(-3 + x)^2}$$

$$\text{Out[110]= } -\frac{x(20 - 9x + x^2)}{(-3 + x)^3}$$

Out[111]= {{x → 0}, {x → 4}, {x → 5}}

$$\text{Out[112]= } \frac{60 - 14x}{(-3 + x)^4}$$

Out[113]= {{x →  $\frac{30}{7}$ }}





```

In[127]:= f = (x^3 - x^2 - x + 1) / ((x - 2)^2)
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -15, 15}]

```

$$\text{Out[127]= } \frac{1 - x - x^2 + x^3}{(-2 + x)^2}$$

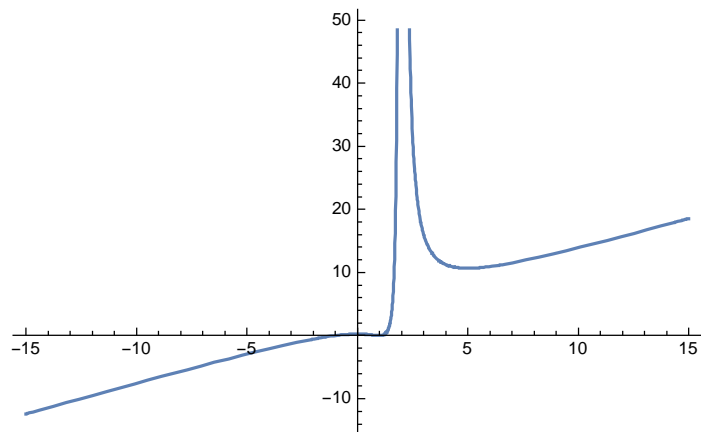
$$\text{Out[128]= } \frac{x(5 - 6x + x^2)}{(-2 + x)^3}$$

Out[129]= {{x → 0}, {x → 1}, {x → 5}}

$$\text{Out[130]= } \frac{2(-5 + 7x)}{(-2 + x)^4}$$

Out[131]= {{x →  $\frac{5}{7}$ }}

Out[132]=



```

In[133]:= f = (-x^3 + 11 x^2 - 44 x + 44) / ((x - 2) ^ 2)
df = D[f, x] // Simplify
Solve[df == 0, x]
ddf = D[df, x] // Simplify
Solve[ddf == 0, x]
Plot[f, {x, -15, 15}]

```

$$\text{Out[133]= } \frac{44 - 44 x + 11 x^2 - x^3}{(-2 + x)^2}$$

$$\text{Out[134]= } -\frac{(-6 + x) x^2}{(-2 + x)^3}$$

Out[135]= {{x → 0}, {x → 0}, {x → 6}}

$$\text{Out[136]= } -\frac{24 x}{(-2 + x)^4}$$

Out[137]= {{x → 0}}

